

multi-party computation

two-party computation \rightarrow possible with fully homomorphic encryption

example:

$$a_0 = a \oplus a_1 \oplus a_2 = 0$$

$$\text{in } \mathbb{F}_2, \quad + \equiv \oplus$$

$$\cdot \equiv \wedge$$

$$a \wedge b = (a_0 \oplus a_1 \oplus a_2) \wedge (b_0 \oplus b_1 \oplus b_2)$$

$$= (a_0 + a_1 + a_2) \cdot (b_0 + b_1 + b_2)$$

$$= a_0 b_0 + a_0 b_1 + a_0 b_2$$

+ ...

only two parties needed per term!

without definitions, it is impossible to determine if something is broken

MPC:

completeness: all parties honest \Rightarrow result correct

fairness: all or no parties receive result

soundness: scheme is 'secure'

requires honest majority

Simulation-based security notion

adversary may corrupt subset of all properties

and can only learn their in-/outputs and some leakage, defined for the functionality
e.g. length of messagecheck whether simulated transcript ^{using ideal functionality} is indistinguishable from real transcriptbits a and b learn $a \wedge b$, nothing elsegive a to Bob, compute $a \wedge b$ secure against active attacker, because choosing $b=1$ gives $a \wedge b = a$
and hence does not 'leak' anything