

chonimity | TCP/IP and TLS → no anonymity; IPsec → anonymity only in tunnel node, after firewalls, gateways

living cryptosystem problem: 3 cryptosystems live, one paid, want to figure out if we are often without realizing who it was. 1. Share pairwise secret bits (between AB, BC, AC) 2. everyone agrees to use a specific XOR of their shared bits 3. if someone paid, they XOR their message with 1 4. broadcast all messages 5. XOR overall messages; result = 0 if no one paid, result = 1 if someone paid

cryptographic message to send message m from A to B, m is sent to the receiver in the format (note: M is the message)

$E_{K_M}(B, E_{K_B}(m))$. M forwards the message to B, who can decrypt it

flushing nodes: message threshold: wait until n messages are received then release all messages. pool size n, probability p. After n messages in pool, shuffle, then add with probability p. Unsent messages leave in pool; stop and go: under determining waiting time for adversary properties: internal/external: can compromise communication medium (internal) and message recipients/knows (internal); passive/active: active can arbitrarily modify computational messages (insert/delete); passive can only liste static/adaptive: static choose compromised resources upfront adaptive can change resources under control during protocol execution

countermeasures against mitm attacks include padding and dummy traffic

In re-encryption protocols, the ciphertext is re-randomized at each node instead of being decrypted. This uses a ~~re-randomizable form of ElGamal~~ scheme. ~~advantage is provability: 1. can prove decryption 2. voting done by user 3. using PKE scheme in the electronic cash~~ conventional cash properties: different values, transferable, anonymous, intrinsically unforgeable, hard to duplicate simple scheme → needs protocol: deposit, payout, withdrawal cut and choose: 1. Create fake checks with random serial numbers and amount. 2. Send envelope (with withdrawer's signature) to bank and tell them amount. 3. Bank opens R-1 envelopes at random and verifies amount. 4. Bank signs remaining envelope, withdraws amount and sends back envelope. 5. User takes out check and verifies signature.

Blind signatures: blind signatures allow to hide the message that is being signed. That is, the signature provided will be blind message b(M), which provides a signature on b(M), from which a signature on M can be extracted. security properties: one more unforgeability: from oracle calls, no worthless valid signatures can be obtained, unlinkability: the signer should be unable to link any particular signature with a specific execution of the signing protocol. (This is possible using RSA signatures)

multiple roots solution: use different public exponents (e_i) to encode different denominations of tokens. As long as e_i are relatively prime, index-calculus-like attacks do not work

off-chain version of the protocol include $y_j = H(x_j)$ and $y_j' = H'(x_j)$ in the bill, where the XOR of x_j and x_j' gives the user's identity. Then use the approach with unfolding R-1 bills again (control of this). If someone attempts to spend a bill twice, (part of) their identity is leaked.

Bitcoin transactions contain many inputs, many outputs. A block includes a chronological ('timestamped') snapshot of all transactions. Proof of work is a defacto distributed timestamping mechanism. Every block is timestamped to about every 10 minutes. Reward work (miner's work) is part of the transaction fees.

homomorphism is a structure-preserving map. ElGamal is a homomorphic encryption scheme, in which multiplying two ciphertexts is equivalent to multiplying the corresponding plaintexts. In general ElGamal, the two ciphertexts are a fixed seed as exponent; i.e. no adm. become no adm^n . This way, when the texts are multiplied, in effect the corresponding plaintexts are added. This requires solving a discrete log to retrieve the plaintext, however, which is doable as long as the number of participants is small.

IND-CCA2 (indistinguishability under adaptive chosen ciphertext attack) security is the achievable for my homomorphic encryption scheme. IND-CCA1 is achieved by ElGamal, in addition to IND-CCA2. Possible homomorphic encryption schemes are semi-randomizable

basic version involves a trusted authority to which all voters are connected, with a box to vote. The system consists of all voters, which due to homomorphic properties can be decrypted to the actual sum of votes. The basic version also assumes that the voters are honest (i.e. for/against). The role of a trusted authority can be disturbed by honesty to the collection of keys of several voters, only the group of voters having the key can decrypt. This does allow for obstruction by a party controlling the whole box, which can be overcome with the following.

Fully homomorphic encryption (FHE) allows doing computation without losing data. Bootstrapping is a process using the encryption of a secret key with its public key. This allows for 'decryption' without knowing the key, and is used by homomorphically reducing the ciphertext to reduce noise in lattice-based communication schemes.

Properties of zero-knowledge proofs: 1. completeness → honest prover proves true statements are accepted. 2. soundness → it is impossible to create valid proof for false statement. 3. zero-knowledge → it can be simulated for false statements such that the result is indistinguishable from a real proof. The Fiat-Shamir heuristic allows for turning interactive ZK proofs to non-interactive ZK proofs (which can be used as protocols), up to the question that random oracles exist. Commitment schemes require two properties: hiding (of the content of the commitment) and binding (so that the content of the commitment cannot be changed). They are deterministic, have less information and don't hide. A random oracle suffices if the message is sufficiently long and random enough. Pedersen commitments are a scheme with common reference string h,g. To commit on $b \in \mathbb{Z}_N$, one samples random t and publishes the commitment $g^m h^{-t} = g^{m+t}$. Under the assumption that h is unknown, this binds. It also achieves information-theoretic hiding.

N-DP (n-party computation) GMW scheme → a scheme which reduces multi-party computation of AND to two-party computation. The circuit contains both AND and XOR, which forms complete set of operations. Oblivious transfer is a method for B to get one of two A without A knowing which B had message he desires. A mechanism exists which only leaves interactive adversary to encrypt/decrypt oracle and violates deal rules. OCB2 forgery: a forgery for OCB2 can be constructed from an encryption oracle query for (N, n, M) , with $M = \text{len}(C_1)/m_2$, where $m_2 = n$. A = E and N is arbitrary. Some modifications allow for extending the attack to longer messages. Some more work allows for constructing universal forger and recovering plaintexts.

Grover's algorithm reduces the brute-force by \sqrt{n} . Introducing new cryptographic sets, and making it very long (N is 256 to 512 bits, 33 years). Naor's algorithm for period finding beats RSA, ECC, DH. Categories of public-key post-quantum systems: code-based encryption based on hardness of decoding error-correcting codes. Pair-based signatures based on hardness of finding second preimage to hash function. Lattice-based encryption based on hardness of finding isogenies between elliptic curves over finite fields. Lattice-based encryption & signatures based on hardness of finding short vectors in some (typically special) lattice. Multivariate-quadratic systems based on hardness of solving systems of multivariate equations over finite fields.

| Name | Signature Function | Hashed commitment | Winner |
|----------|--------------------|---------------------|------------------------------------|
| Tiger | KEM | structured lattices | which takes t_1, t_2, f as input |
| Althheim | signature scheme | structured lattices | t_2, f as input |
| Edem | commitment scheme | structured lattices | which takes t_1, t_2, f as input |
| SPHINX | signature scheme | hash functions | t_1, t_2, f as input |
| BIKE | KEM | codes | t_1, t_2, f as input |
| Resphinc | KEM | codes | t_1, t_2, f as input |
| HQC | KEM | codes | t_1, t_2, f as input |
| SIKE | KEM | isogenies | t_1, t_2, f as input |

It is possible for a scheme to be secure against active attacks while being insecure against passive attackers.

requires storing 2^w one-time secret keys, both can be optimized by selecting them from a (short) seed. The scheme calls for a static key by using it to sign other keys to expand the key space. This idea was due to Goldreich & Levin. Winternitz signature: each chain runs for 2^w steps. For signing 256-bit hash, the keys $t_1, \dots, t_{2^{w-1}}$ and $C = \sum_{i=1}^{2^w} t_i C_i$ in base 2^w ($C_i \in \mathbb{Z}_{2^w}$) are needed. Only the top node needs to be revealed as the public key for the whole chain. The public key is one node below the top node of the chain. The public key is C .